

WEEK 1.2 Friday project

$$n_{ice} = \sqrt{\frac{2 K_{ice}}{\rho_{ice} L} \underbrace{\Delta T \Delta t}_{f} + h_0^2} = \left[f \cdot \Delta T \Delta t + h_0^2 \right]^{1/2}$$

$$\frac{\partial n_{ice}}{\partial \Delta T} = \frac{1}{2} \left[f \cdot \Delta T \Delta t + h_0^2 \right]^{-1/2} \cdot f \Delta t$$

$$\begin{aligned} \frac{\partial^2 n_{ice}}{\partial^2 \Delta T} &= \frac{f \Delta t}{2} \cdot \left[\frac{-1}{2} \right] \left[f \cdot \Delta T \Delta t + h_0^2 \right]^{-3/2} \cdot f \Delta t \\ &= -\frac{f^2 \Delta t^2}{4} \left[f \cdot \Delta T \Delta t + h_0^2 \right]^{-3/2} \end{aligned}$$

$$\frac{\partial n_{ice}}{\partial h_0} = \frac{1}{2} \left[f \cdot \Delta T \Delta t + h_0^2 \right]^{-1/2} \cdot 2 h_0 = h_0 \left[\right]^{-1/2}$$

$$\begin{aligned} \frac{\partial^2 n_{ice}}{\partial^2 h_0} &= \left[f \Delta T \Delta t + h_0^2 \right]^{-1/2} + h_0 \left[\frac{-1}{2} \right] \left[f \Delta T \Delta t + h_0^2 \right]^{-3/2} \cdot 2 h_0 \\ &= \left[f \Delta T \Delta t + h_0^2 \right]^{-1/2} - h_0^2 \left[f \Delta T \Delta t + h_0^2 \right]^{-3/2} \end{aligned}$$